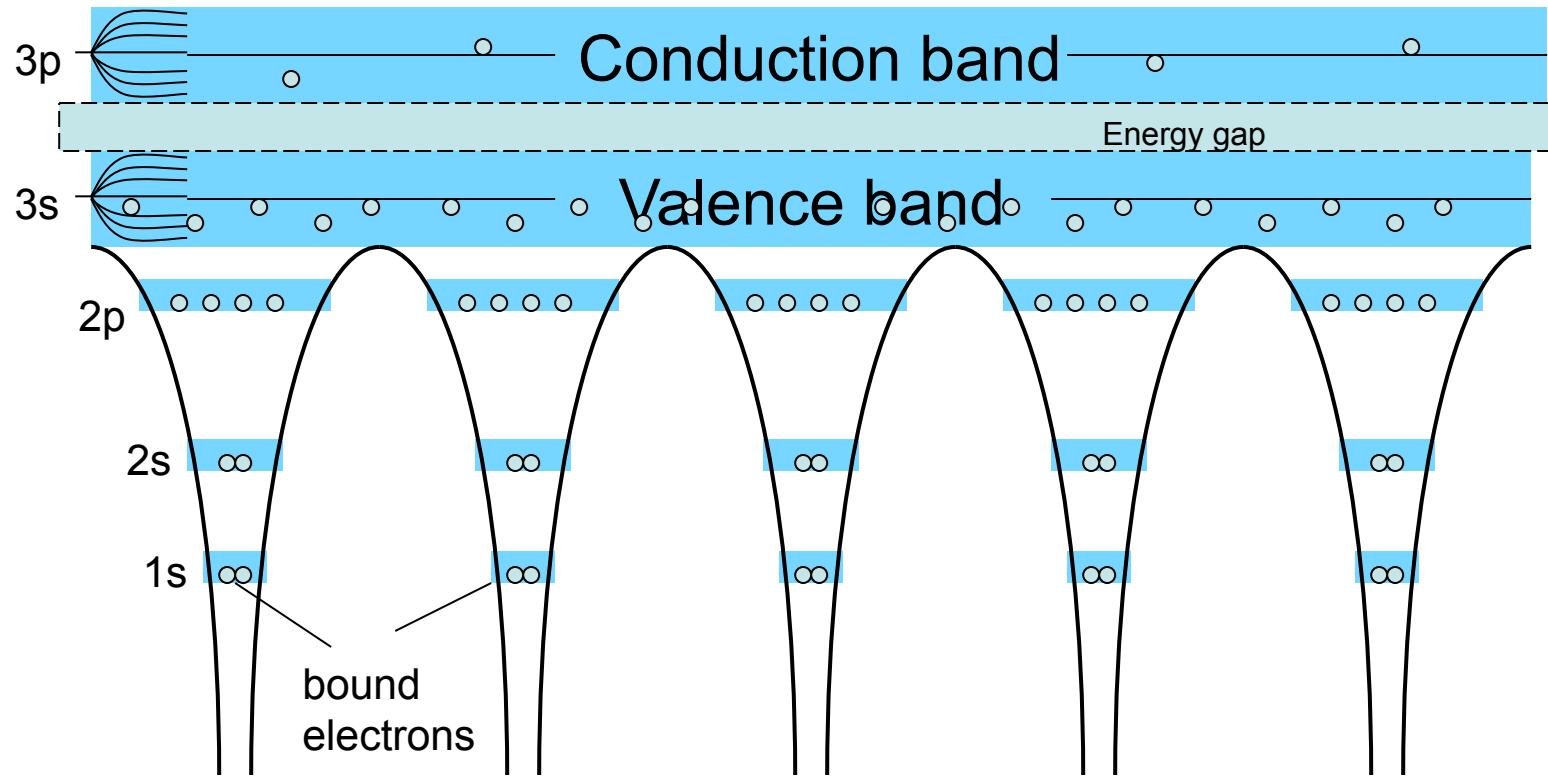


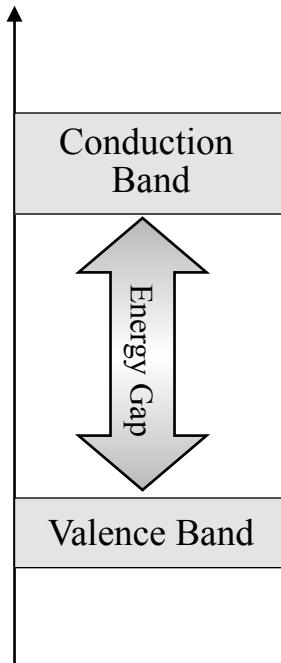
# Electrons in Solids



When atoms form a crystalline structure (metals, semiconductors, ) the valence electrons loose their attraction to a local atom and form an band of ~equivalent charges- **valence band**. The **conduction band** lies within or above the valence band.

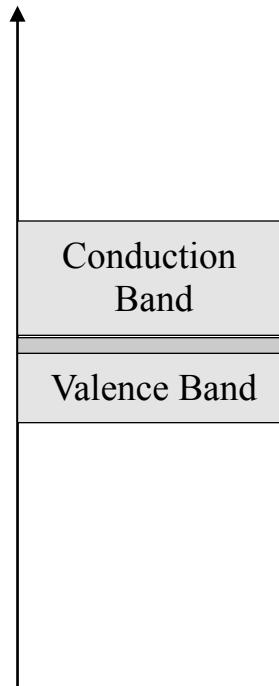
# Energy Bands

Electron Energy



Insulator

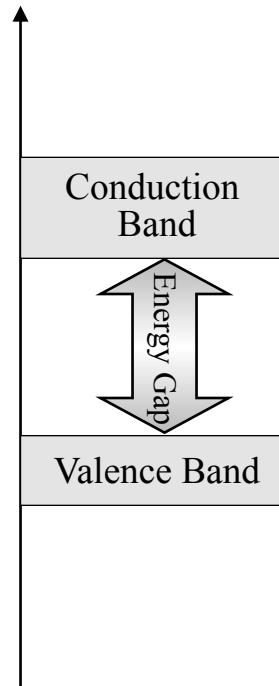
Electron Energy



Conductor

Overlapping bands  
- little energy is  
needed for  
conduction

Electron Energy

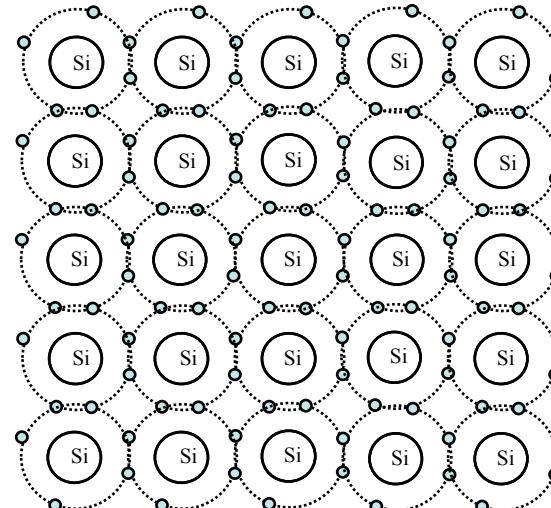


Semiconductor

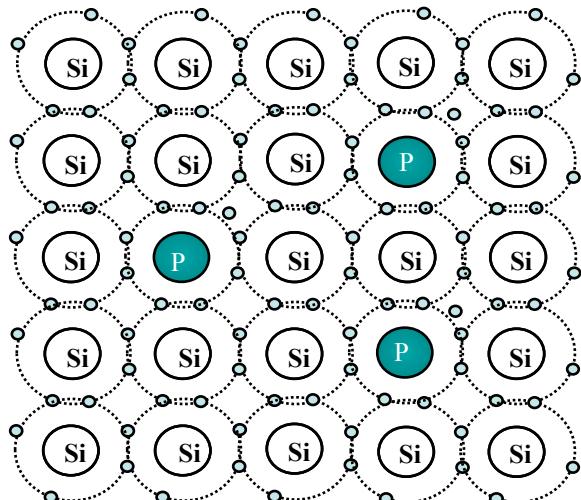
# Semiconductors and Impurity Dopants

5 <b>B</b> Boron 2.34	6 <b>C</b> Carbon 2.62	7 <b>N</b> Nitrogen 1.251
13 <b>Al</b> Aluminum 2.70	14 <b>Si</b> Silicon 2.33	15 <b>P</b> Phosphorus 1.82
31 <b>Ga</b> Gallium 5.91	32 <b>Ge</b> Germanium 5.32	33 <b>As</b> Arsenic 5.72

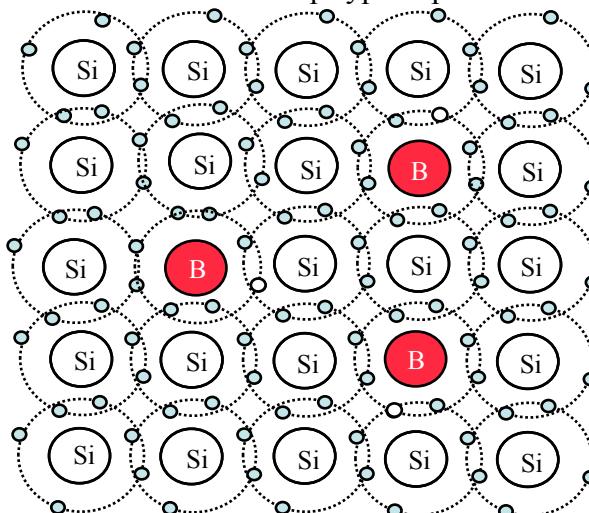
Silicon atoms share valence electrons to form insulator-like bonds.



Phosphorus atom serves as n-type dopant

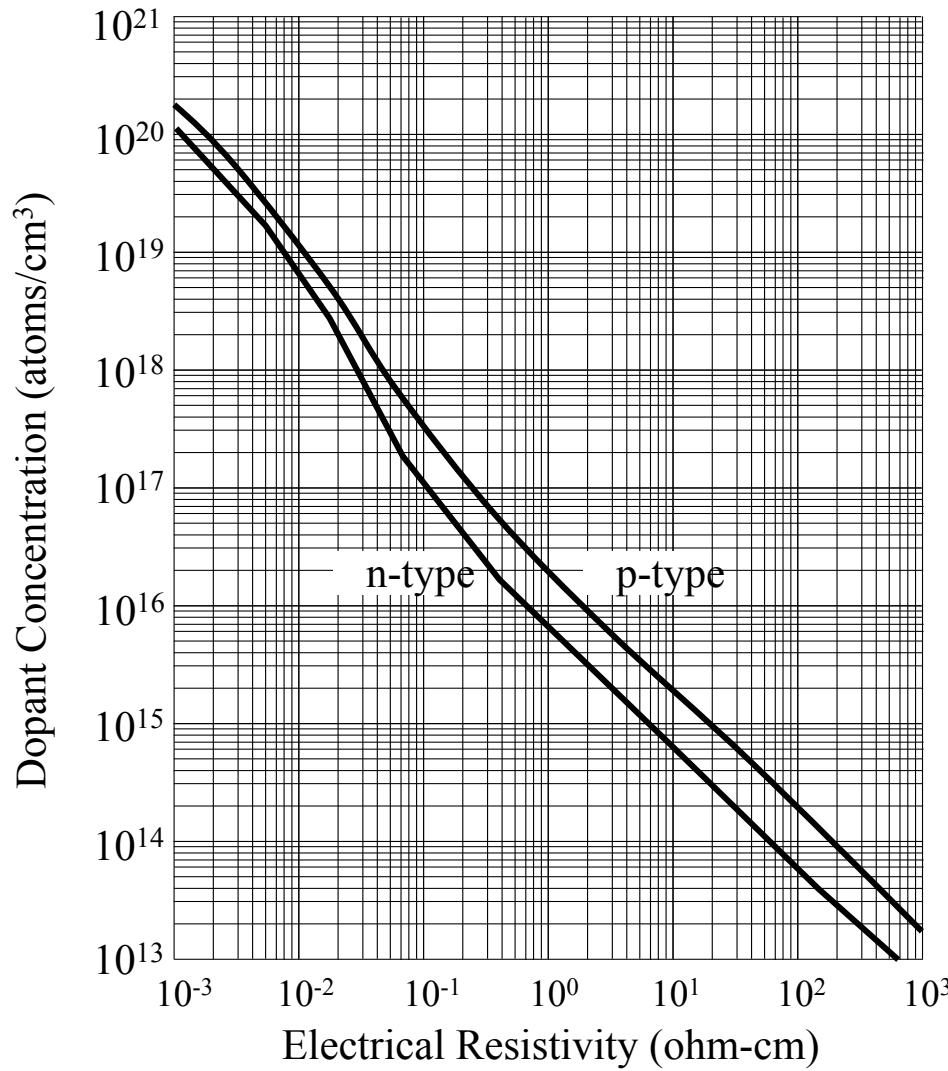


Boron atom serves as p-type dopant

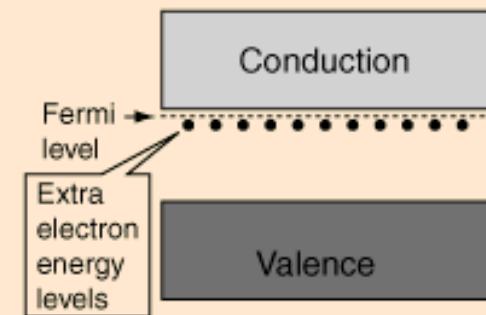


# Silicon Resistivity Versus Dopant Concentration

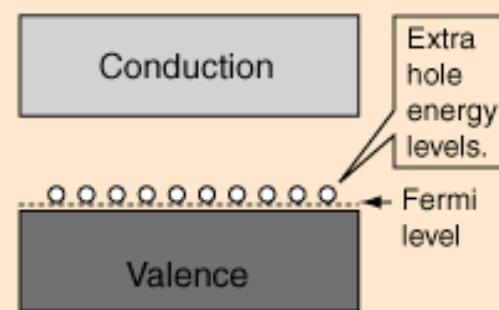
<http://hyperphysics.phy-astr.gsu.edu/hbase/Solids/dope.html>



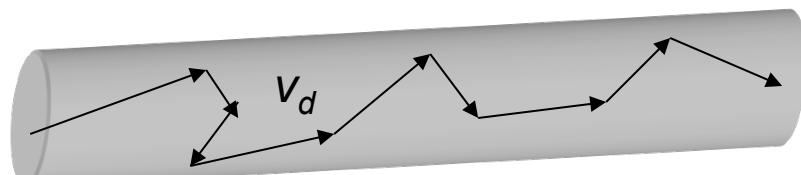
The addition of pentavalent impurities such as antimony, arsenic or phosphorous contributes free electrons, greatly increasing the conductivity of the intrinsic semiconductor. Phosphorous may be added by diffusion of phosphine gas (PH<sub>3</sub>).



The addition of trivalent impurities such as boron, aluminum or gallium to an intrinsic semiconductor creates deficiencies of valence electrons, called "holes". It is typical to use B<sub>2</sub>H<sub>6</sub> diborane gas to diffuse boron into the silicon material.

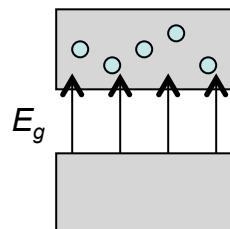


# Resistivity $\rho = 1/\sigma$



$$\rho_m = \frac{m}{ne^2} \frac{1}{\tau}$$

- $j = n q v$  ( $A/m^2$ ) current density
- $E = j \cdot \rho$  Ohm's Law  
 $(j = I/A \quad R = \rho \cdot (L/A) \quad E = V/L)$
- Electrons will collide on average  $\tau$  seconds apart.  
 $\tau \equiv$  collision time (relaxation time)
- Drift velocity of electrons  $v_d = a \cdot \tau = \frac{qE}{m} \cdot \tau$
- $\rho = \frac{E}{j} = \frac{m}{ne^2} \frac{1}{\tau} = \frac{m}{ne^2} \left( \frac{1}{\tau_{\text{crystal}}} + \frac{1}{\tau_{\text{impurities}}} \right)$



## SEMICONDUCTOR

$$\rho_{sc} = \rho_m (T / T_0)^{-3/2} e^{E_g / 2kT}$$

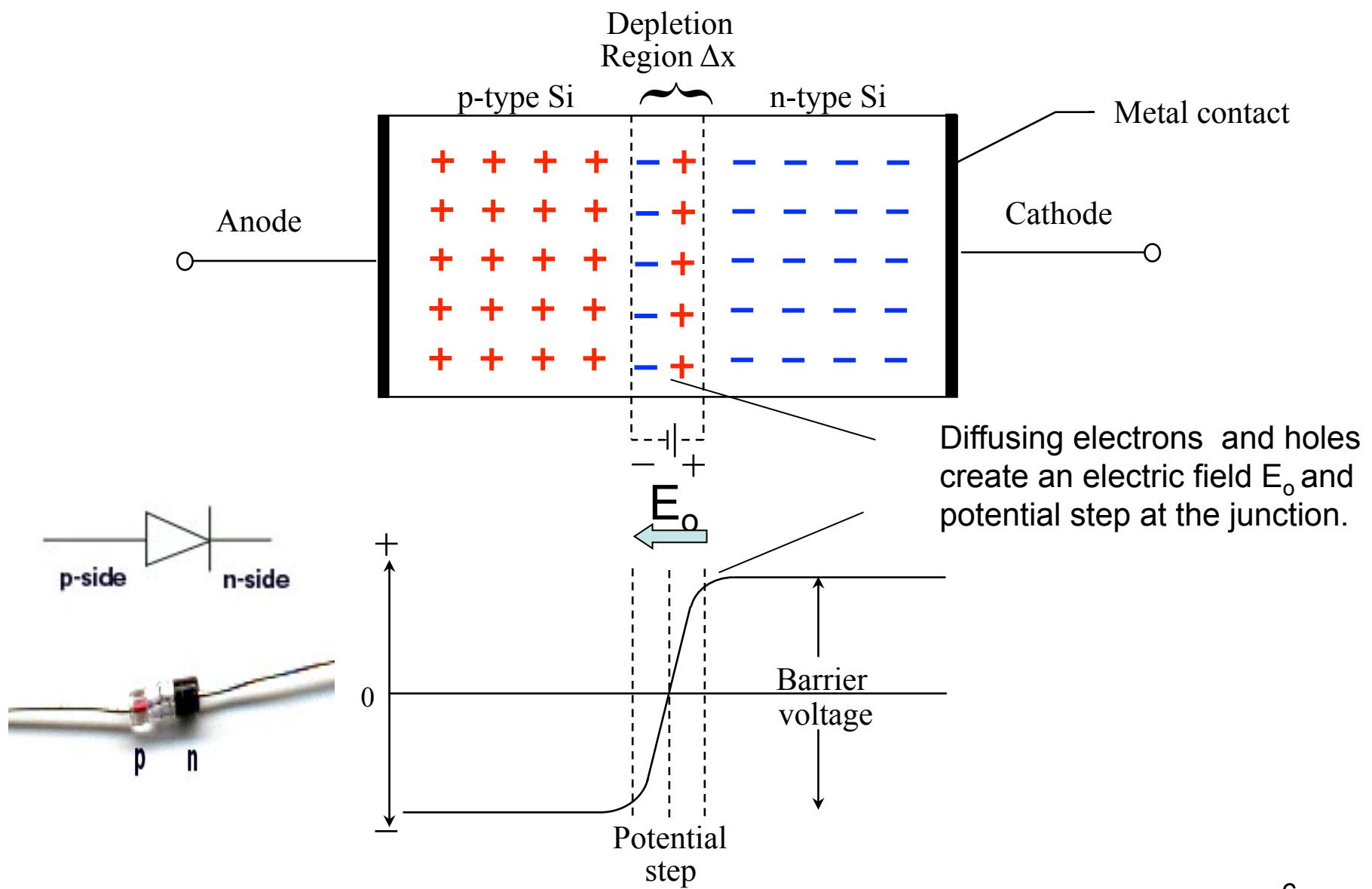


## DIODE or PN JUNCTION

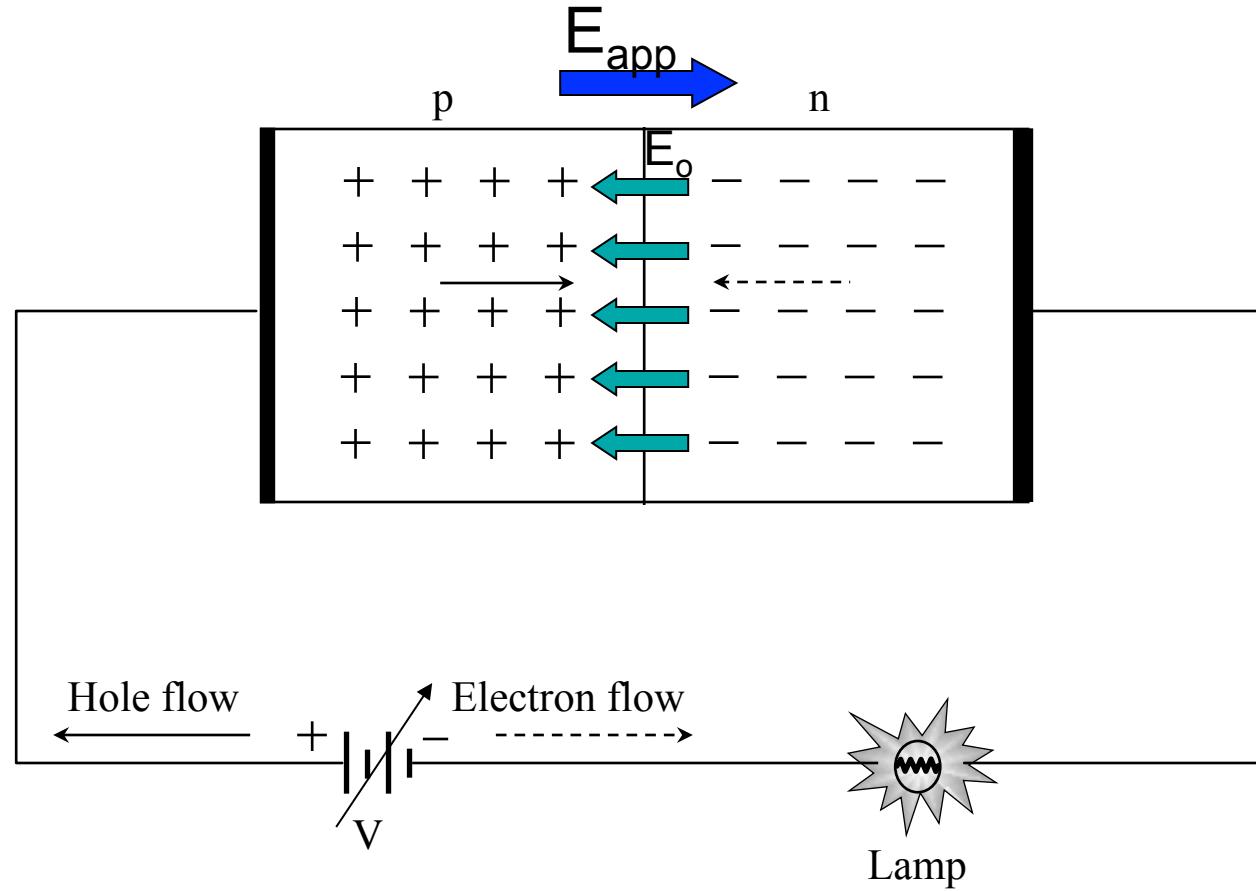
$$I = I_0 [e^{eV/kT} - 1]$$



## Diode Action

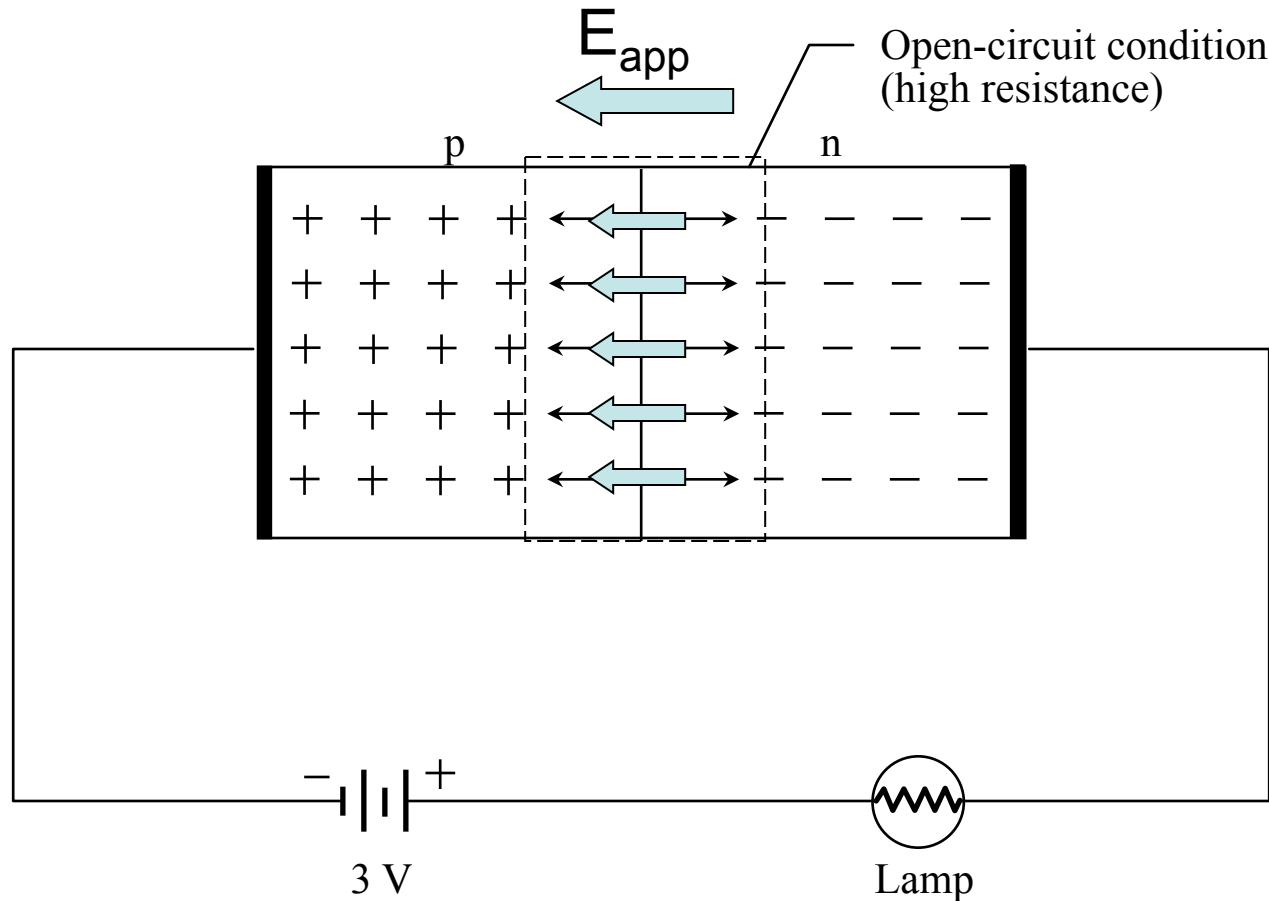


## Forward-Biased PN Junction Diode



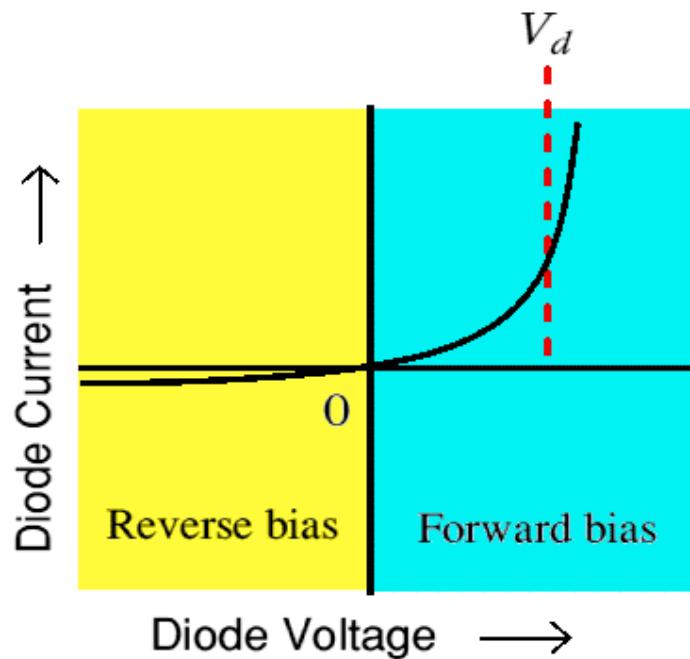
In **forward bias** the applied E-field cancels internal electric field and charges begin flowing across the junction when  $E_{app} > E_o$  or  $V_{app} > \sim 0.6V$ .

# Reverse-Biased PN Junction Diode



In the **reverse bias** the external E-field increases the size of the depletion zone until all charge carriers are near the contacts - **fully depleted**.

# Diodes



$$I = I_0 \left( \text{Exp} \left\{ \frac{eV}{kT} \right\} - 1 \right)$$

$I$  = Current through diode in Amps

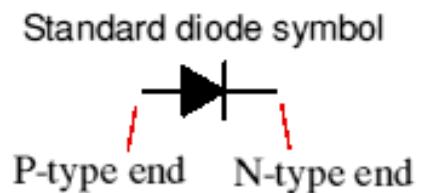
$I_0$  = The diode's 'Saturation Current' value

$e$  = electron charge,  $1.602 \times 10^{-19}$  C

$T$  = temperature in degrees Kelvin

$V$  = Applied voltage in Volts

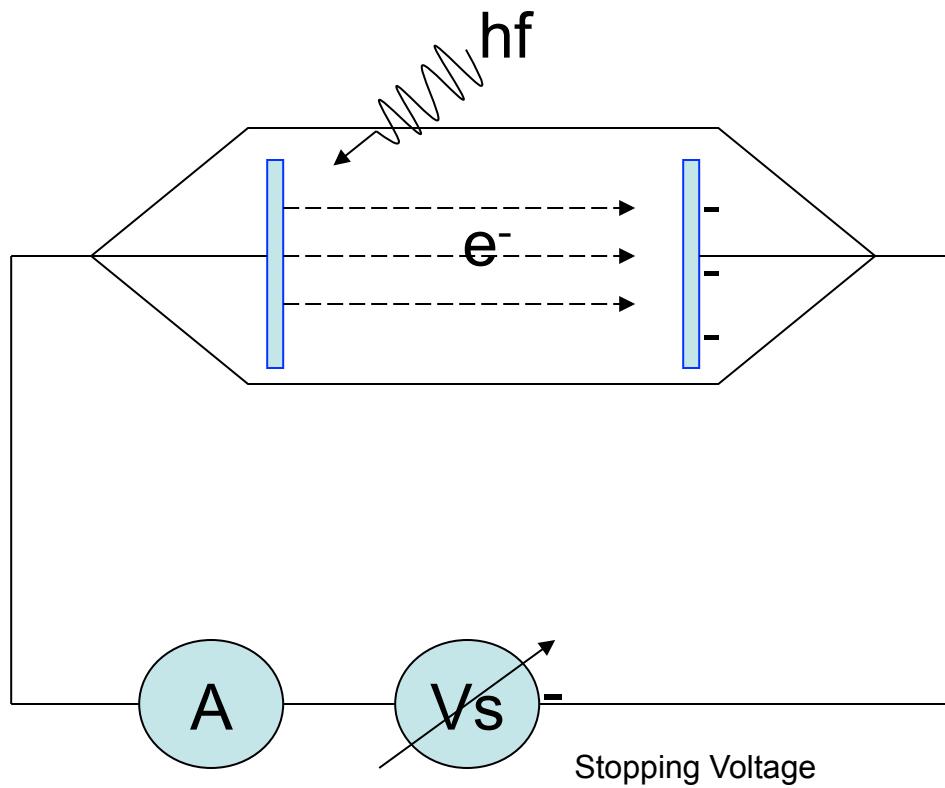
$k$  = Boltzmann's constant,  $1.380 \times 10^{-23}$  J/K



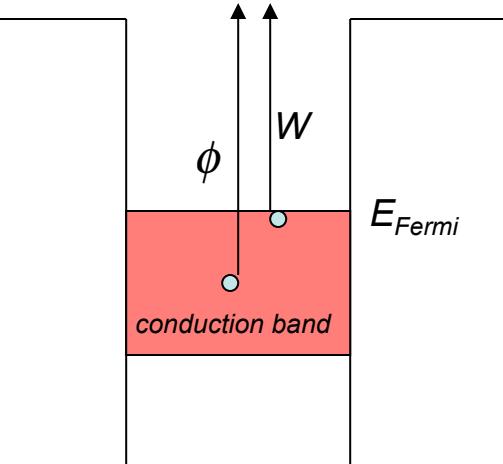
## DIODE or PN JUNCTION

$$I = I_0 \left[ e^{e(V-V_g)/kT} - 1 \right] = I_0 e^{(V-V_g)/kT}$$

# Photo-Electric Effect in a Metal

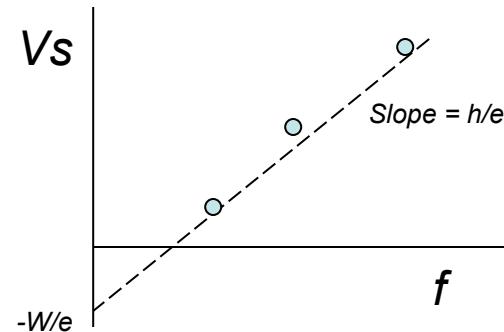


$$KE = hf - \phi$$

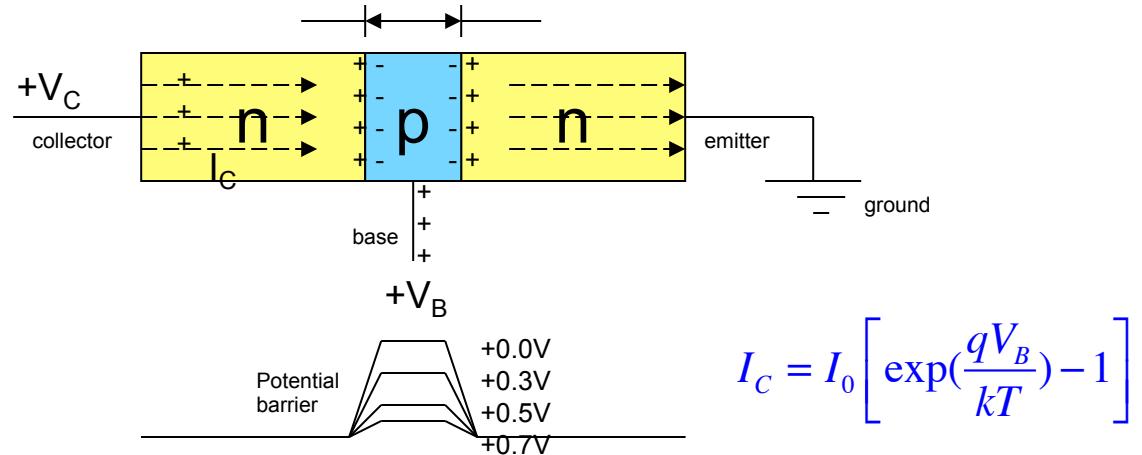


$$KE_{max} = eV_s = hf - W$$

$W \equiv$  work function of the metal



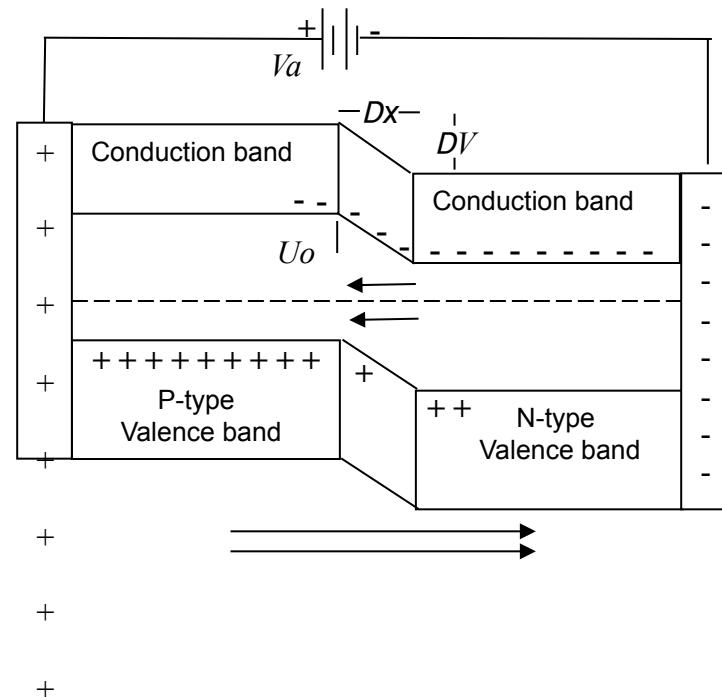
# Transistor Action



- A transistor is constructed by opposing two diodes structures n-p-n or p-n-p.
- No collector current can flow through the collector-base junction (reverse diode).
- By increasing the base voltage  $+V_B$  to about +0.7V the potential barrier is lowered and a large collector current can cross to ground ( $\rho_{\text{transistor}} \rightarrow 0$ ).
- By modulating the  $V_B$  one can form an amplifier  $A=I_C/I_B$ . (Analogue electronics)
- If  $V_B \gg 1V$  then the transistor saturates to a digital pulse (Digital electronics).

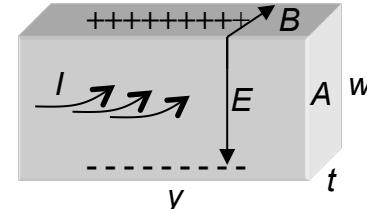
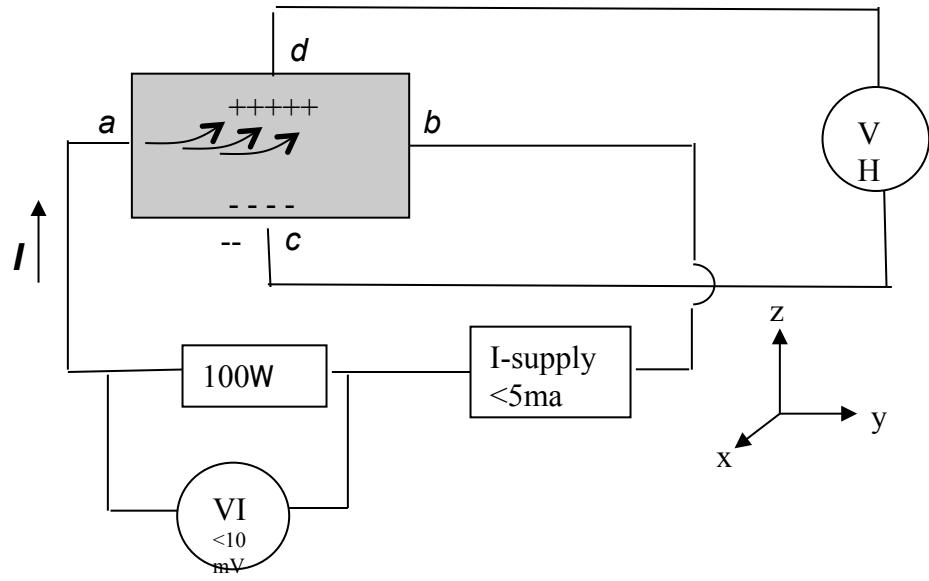
# Light Emitting Diodes

- A PN junction is characterized by a contact diffusion voltage  $U_0$  which develops across the diode depletion zone.
- In forward bias condition electrons and holes can annihilate in the zone emitting a photon of energy  $hf = U_0$ .  $U_0$  can be engineered to produce different color emissions.
- An LED is special in that the diode is transparent to this photon emission. In a normal diode e-p annihilation energy returns to heating the diode.



Color	Wavelength (nm)	Voltage (V)	Semiconductor Material
Infrared	$\lambda > 760$	$\Delta V < 1.9$	Gallium arsenide (GaAs) Aluminium gallium arsenide (AlGaAs)
Red	$610 < \lambda < 760$	$1.63 < \Delta V < 2.03$	Aluminium gallium arsenide (AlGaAs) Gallium arsenide phosphide (GaAsP) Aluminium gallium indium phosphide (AlGaNp) Gallium(III) phosphide (GaP)
Orange	$590 < \lambda < 610$	$2.03 < \Delta V < 2.10$	Gallium arsenide phosphide (GaAsP) Aluminium gallium indium phosphide (AlGaNp) Gallium(III) phosphide (GaP)
Yellow	$570 < \lambda < 590$	$2.10 < \Delta V < 2.18$	Gallium arsenide phosphide (GaAsP) Aluminium gallium indium phosphide (AlGaNp) Gallium(III) phosphide (GaP)
Green	$500 < \lambda < 570$	$1.9^{[32]} < \Delta V < 4.0$	Indium gallium nitride (InGaN) / Gallium(III) nitride (GaN) Gallium(III) phosphide (GaP) Aluminium gallium indium phosphide (AlGaNp) Aluminium gallium phosphide (AlGaP)
Blue	$450 < \lambda < 500$	$2.48 < \Delta V < 3.7$	Zinc selenide (ZnSe) Indium gallium nitride (InGaN) Silicon carbide (SiC) as substrate Silicon (Si) as substrate — (under development)
Violet	$400 < \lambda < 450$	$2.76 < \Delta V < 4.0$	Indium gallium nitride (InGaN)
Purple	multiple types	$2.48 < \Delta V < 3.7$	Dual blue/red LEDs, blue with red phosphor, or white with purple plastic
Ultraviolet	$\lambda < 400$	$3.1 < \Delta V < 4.4$	diamond (235 nm) <sup>[33]</sup> Boron nitride (215 nm) <sup>[34][35]</sup> Aluminium nitride (AlN) (210 nm) <sup>[36]</sup> Aluminium gallium nitride (AlGaN) Aluminium gallium indium nitride (AlGaN) — (down to 210 nm) <sup>[37]</sup>
White	Broad spectrum	$\Delta V = 3.5$	Blue/UV diode with yellow phosphor

# Hall Effect in p-Germanium



$$\vec{j} = nq\vec{v}_d \quad \text{current density} = I / \text{area}$$

$$m \frac{\vec{v}_d}{\tau} = q(\vec{E} + \vec{v}_d \times \vec{B}) = 0 \quad \text{equilibrium}$$

$$E_z = -v_d^\ell B_x \rightarrow V_y / w = \frac{I}{wt} \frac{1}{nq} B_x$$

$$V_H = \left( \frac{B_x}{nq t} \right) I \quad \text{Hall Voltage}$$

$$R_H = \frac{E_z}{j_y B_x} = \frac{1}{nq} \quad \text{Hall Coefficient}$$

- $n$  is the number of free charge carriers in the sample.
- In a semiconductor the free charge carriers  $n$  are both electrons and holes.
- By measuring the Hall voltage  $V_H$  vs  $I$  at a known value of  $B$  we can measure  $n$  for the sample.
- Slope =  $(1/nq)(B/t)$  where  $R_H = 1/nq$ .
- Since  $B = t \times I / R_H$  one can use the Hall effect to measure magnetic fields - Hall Probe!